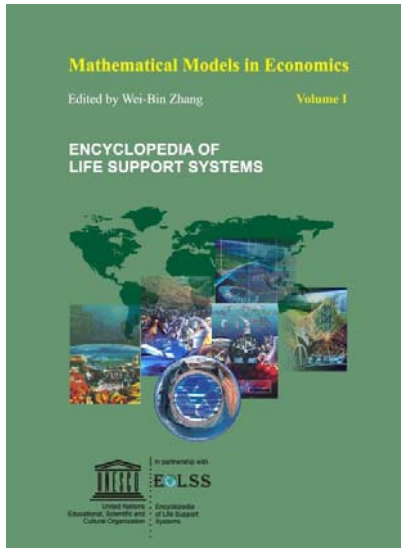


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MATHEMATICAL MODELS IN ECONOMICS



Mathematical Models in Economics - Volume 1

No. of Pages: 542

ISBN: 978-1-84826-228-7 (eBook)

ISBN: 978-1-84826-678-0 (Print Volume)

Mathematical Models in Economics - Volume 2

No. of Pages: 521

ISBN: 978-1-84826-229-4 (eBook)

ISBN: 978-1-84826-679-7 (Print Volume)

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