# **OPTIMAL CONTROL WITH FEMTOPULSES: THEORY AND EXPERIMENTS**

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#### Summary

The ideal excitation source for study molecular dynamics, to control the dynamics of atomic, molecular, and solid-state systems, and to drive them into novel, non-equilibrium states is femtosecond laser pulse because of its ultrahigh laser intensity and ultra-short pulse duration. Phase shaping is widely used in femtosecond pulses to achieve the optimal coherent control in femtosecond laser experiments. In the present chapter, two specific applications are taken as examples to demonstrate the potential application of optimal control with femtosecond pulses. One is the optimal control in Coherent Anti-Stokes Raman Scattering (CARS), and control methods can be employed here to improve the chemical selectivity in CARS spectroscopy and spatial resolution in CARS microscopy. The other is about how to obtain the optimal control mechanisms in experiments.

#### **1. Introduction**

Femtosecond laser pulse is considered as an ideal excitation source because of its ultrahigh laser intensity and ultrashort pulse duration. As an important technology, femtosecond pulse shaping is to obtain a desired pulse by controlling the pulse amplitude, phase, and polarization direction. Up to now, it has been widely used in the areas of molecular dynamics, nonlinear spectroscopy, femtosecond chemistry, biomedical imaging and quantum computation (Weiner, 2000; Brif et al, 2010; Goswami, 2003; Weiner, 2011).



Figure 1. One typical 4-F pulse shaper experimental setup for Fourier Transform pulse shaping.

4-F pulse shaper is mostly commonly adopted as the pulse shaping apparatus in the experiment. As shown in Figure 1, the setup can perform pulse shaping via Fourier Transform. It usually consists of a pair of diffraction gratings and lenses and one mask located in the middle position. The distances between adjacent components are all F, which is the focal length of the lens. That is just why we call this apparatus 4-F pulse shaper. The lenses can also be replaced with concave mirrors, which does not change its principle described in the following. Firstly, the individual frequency components in the input pulse are angularly diffracted by the first grating, and then focused to small diffraction limited spots at the back focal plane of the first lens, where the mask is placed. Thus the frequency components are spatially separated along one dimension in the mask, which can been as a Fourier Transform from the time domain to the frequency domain. Spatially patterned amplitude and phase masks (or a Spatial Light Modulator, SLM) are placed in this plane in order to manipulate the spatially dispersed optical Fourier components.

The pixels in the mask can have different optical properties such as refractive indices to modulate the corresponding incident frequency components. After the mask, the second lens and grating recombine all the frequencies into a single beam to obtain a shaped output pulse. This could be seen as a Fourier Transform from the frequency domain to the time domain. In the 4-F pulse shaper apparatus, the pulse shaping is done via the modulation mask. If the mask performs no modulation, then the output pulse is the same as the input pulse.

Quantum control can be performed with 4-F pulse shaper in femtosecond laser experiments. In the following, two specific applications are taken as examples to demonstrate the potential application of optimal control with 4-F femtosecond pulse shaper. One is the optimal control in coherent anti-Stokes Raman Scattering (CARS), where control methods are employed to improve the chemical selectivity in CARS spectroscopy and spatial resolution in CARS microscopy. The other is about how to obtain the optimal control mechanisms.

Coherent anti-Stokes Raman Scattering, as a four-wave nonlinear process, has been widely used to study chemical systems in solutions, reactions in the gas phase, and

vibrational dynamics in gas and condensed phases. As shown in Figure 2, the pump and Stokes pulses generate coherence between two vibrational levels, when they have a frequency difference which coincides with the Raman resonance  $\Omega_R$ . The probe pulse then induces the anti-Stokes signal. Thus it can be employed to label biological samples with certain Raman transitions.



Figure 2. Energy level diagram of the CARS process. The left and right panels correspond to the resonant and non-resonant background contributions, respectively. Three pulses are employed in the process: the pump, Stokes and probe pulses. The solid lines indicate the vibrational levels of the system, while the dotted lines mean virtual states. Reproduced from [Gao et al, 2012], with the permission of AIP Publishing.

CARS microscopy, pioneered by Duncan *et al* (1982) and developed by Xie *et al*, is widely used to image biological species. As a combination of ultrafast nonlinear spectroscopy and microscopy, CARS microscopy is a highly chemically selective and sensitive technique that employs a CARS signal of an unlabeled sample and provides higher spatial resolution. Figure 3 (Cheng et al, 2002) shows four typical configurations of CARS microscopies, and the pulse shaper can of course be added before the first objective lens to modulate the pump or probe pulse. In these microscopies, the pump pulse  $\omega_p$  is also used as the probe pulse. The temporally and spatially overlapped pump and Stokes laser pulses are tightly focused into a sample to generate a signal in a small excitation volume (<1  $\mu$ m<sup>3</sup>). A CARS image is acquired by raster scanning the sample or the laser beams. The vibrational contrast in CARS microscopy arises from the signal enhancement when  $\omega_p - \omega_s$  is tuned to a Ramanactive vibrational band.

The femtosecond laser pulse-shaping technique can be integrated into a 'closed-loop learning' scheme to perform quantum control (see Figure 4). The scheme proposed by Judson and Rabitz (1992) has been employed in many femtosecond laser experiments to control the dynamics in a variety of systems of interest. Figure 4 shows a typical 'closed-loop learning' scheme (Rabitz et al, 2000). The loop is entered with an initial field. Then a laser control field design is done by the learning algorithm and the pulse shaper. After that, the modulated pulse will act with the sample in the experiment, and the results will be assessed and fed to the algorithm to suggest an improved field design. These steps are repeated until the objective is achieved. The scheme is a kind of feedback control and can identify the best shapes of femtosecond laser control pulses for steering quantum dynamics towards the desired target. The mechanisms under the

shaped pulses in the experiment are usually complex, and the Rabitz group has proposed a method called Hamiltonian encoding-observable decoding (HE-OD) to unveil the control mechanisms. This method often can be implemented with only software changes guiding the laser apparatus of many "closed-loop learning" experiments, and the details will be given in Section 2.1.



Figure 3. Four types of CARS microscopies: forward-detected CARS (F-CARS), forward-detected polarization CARS (P-CARS), epidetected CARS (E-CARS) and counter-propagating CARS (C-CARS). P, polarizer; OL, objective lens; S, sample; F, filter; HW, half-wave plate; D, dichroic mirror. Reproduced from [Cheng et al, 2002], with the permission of OSA Publishing.



Figure 4. A 'closed-loop learning' scheme for teaching a laser to control quantum systems.

## 2. Optimal Control in Coherent anti-Stokes Raman Scattering (CARS)

Usually picosecond pulses are used in CARS spectroscopy and microscopy, and its narrow bandwidth is adequate to detect specific Raman bands. Additionally, the non-resonant background is greatly suppressed. However, when investigating broadband CARS spectra, especially in the Raman fingerprint region which spans from 800 to 1800 cm<sup>-1</sup>, we have to bring in broadband femtosecond pulses. In this case, the non-resonant background may become significant. Therefore, optimal control is necessary

to simultaneously enhance the resonant signal and suppress the non-resonant background (Gao et al, 2012).

### 2.1. Optimal Control in CARS Spectroscopy

The CARS signal  $I_{\text{CARS}}(\tilde{\omega}_{as})$  is a coherent superposition of resonant third-order nonlinear polarization  $P_r^{(3)}(\tilde{\omega}_{as})$  and non-resonant third-order nonlinear polarization  $P_{nr}^{(3)}(\tilde{\omega}_{as})$ ,  $I_{\text{CARS}}(\tilde{\omega}_{as}) = |P_r^{(3)}(\tilde{\omega}_{as}) + P_{nr}^{(3)}(\tilde{\omega}_{as})|^2$  with

$$P_{\rm r}^{(3)}(\tilde{\omega}_{\rm as}) = \iiint_{-\infty}^{\infty} d\tilde{\omega}_{\rm p} d\tilde{\omega}_{\rm s} d\tilde{\omega}_{\rm pr} \frac{C}{\Omega_{\rm R} - (\tilde{\omega}_{\rm p} - \tilde{\omega}_{\rm s}) - i\Gamma} \tilde{E}_{\rm p}(\tilde{\omega}_{\rm p}) \tilde{E}_{\rm s}^{*}(\tilde{\omega}_{\rm s}) \tilde{E}_{\rm pr}(\tilde{\omega}_{\rm p}) \delta(\tilde{\omega}_{\rm as} - \tilde{\omega}_{\rm p} + \tilde{\omega}_{\rm s} - \tilde{\omega}_{\rm pr}),$$

$$P_{\rm nr}^{(3)}(\tilde{\omega}_{\rm as}) = \iiint_{-\infty}^{\infty} d\tilde{\omega}_{\rm p} d\tilde{\omega}_{\rm s} d\tilde{\omega}_{\rm pr} \chi_{\rm nr} \tilde{E}_{\rm p}(\tilde{\omega}_{\rm p}) \tilde{E}_{\rm s}^{*}(\tilde{\omega}_{\rm s}) \tilde{E}_{\rm pr}(\tilde{\omega}_{\rm p}) \delta(\tilde{\omega}_{\rm as} - \tilde{\omega}_{\rm p} + \tilde{\omega}_{\rm s} - \tilde{\omega}_{\rm pr}).$$

Here  $\Omega_{\rm R}$  is the Raman frequency between energy levels 1 and 2,  $2\Gamma$  is the level width, *C* is a constant which depends on the material property, and  $\chi_{\rm nr}$  is the non-resonant third-order susceptibility.

The pulses employed in laser experiments are usually of the Gaussian form:

$$\tilde{E}_{k}(\tilde{\omega}_{k}) = \frac{E_{k}}{\Delta_{k}^{1/2}} e^{-(\tilde{\omega}_{k} - \Omega_{k})^{2}/\Delta_{k}^{2}} e^{i\Phi_{k}(\tilde{\omega}_{k} - \Omega_{k})}, k = \{\text{p,s,pr}\},\$$

where  $2\sqrt{\ln 2\Delta_k}$  is the corresponding spectral full width at half maximum (FWHM), and  $\Phi_k(\tilde{\omega}_k - \Omega_k)$  is the frequency-domain phase profile. For simplicity, the translation  $\omega_k = \tilde{\omega}_k - \Omega_k$  is made. Different phase strategies can be adopted to achieve local optimal control or broadband optimal control.

If we just want to maximize the resonant signal or minimize the non-resonant background at  $\omega_{as} = 0$ , that is,  $\tilde{\omega}_{as} = \Omega_{as}$ , the answer is easy to be obtained. The first three cases in the following are for this kind of control, namely, local optimal control.

Case 1: All the three pulses are shaped for local optimal control at  $\omega_{as} = 0$ . This is the case in three-pulse CARS. We have

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$$\begin{aligned} |P_{\rm r}^{(3)}| &= |\int_{-\infty}^{\infty} \frac{C}{\omega_{\rm pr} - i\Gamma} E_{\rm pr}(\omega_{\rm pr}) [\int_{-\infty}^{\infty} E_{\rm p}(\omega_{\rm p}) E_{\rm s}^{*}(\omega_{\rm p} + \omega_{\rm pr}) d\omega_{\rm p}] d\omega_{\rm pr}| \\ &= |\frac{1}{\Delta^{3/2}} \int_{-\infty}^{\infty} \frac{C}{\omega_{\rm pr} - i\Gamma} e^{-\frac{3\omega_{\rm pr}^{2}}{2\Delta^{2}} + i\Phi_{\rm pr}(\omega_{\rm pr})} A(\omega_{\rm p}, \omega_{\rm pr}) d\omega_{\rm pr}| \\ &\leq |\frac{1}{\Delta^{3/2}} \int_{-\infty}^{\infty} \frac{C}{\omega_{\rm pr} - i\Gamma} e^{-\frac{3\omega_{\rm pr}^{2}}{2\Delta^{2}} + i\Phi_{\rm pr}(\omega_{\rm pr})} ||A(\omega_{\rm p}, \omega_{\rm pr})| d\omega_{\rm pr}| \\ &\leq |\frac{1}{\Delta^{3/2}} \int_{-\infty}^{\infty} \frac{C}{\omega_{\rm pr} - i\Gamma} e^{-\frac{3\omega_{\rm pr}^{2}}{2\Delta^{2}} + i\Phi_{\rm pr}(\omega_{\rm pr})} ||g\sqrt{\frac{\pi}{2}} \Delta g d\omega_{\rm pr}| \\ & (\text{when } \Phi_{\rm p}(\omega_{\rm p}) = \text{cons}, \quad \Phi_{\rm s}(\omega_{\rm s}) = \text{cons}) \\ &\leq C\sqrt{\frac{\pi}{2\Delta}} e^{\frac{3\Gamma^{2}}{4\Delta^{2}}} \text{Bessel} K(0, \frac{3\Gamma^{2}}{4\Delta^{2}}) \\ & (\text{when } \Phi_{\rm pr}(\omega_{\rm pr}) = \arctan(\omega_{\rm pr}/\Gamma) + \text{cons}) \end{aligned}$$

Here K is a modified Bessel function. Thus the optimal phase to enhance the resonant signal is  $\Phi_{\rm pr}(\omega_{\rm pr}) = \arctan(\omega_{\rm pr}/\Gamma) + \cosh$  with pump and Stokes pulses being unshaped transform limited pulses (TLPs). While for the non-resonant background, we

have 
$$P_{\rm nr}^{(3)} = \chi_{\rm nr} \sqrt{\frac{\pi}{2\Delta}} \int_{-\infty}^{\infty} d\omega_{\rm pr} e^{-\frac{3\omega_{\rm pr}^2}{2\Delta^2}} e^{i(\Phi_{\rm pr}(\omega_{\rm pr}))}$$

So the non-resonant background will reach its minimal value of zero when  $\Phi_{pr}(\omega_{pr})$  is the  $\Pi$  step phase function about  $\omega_{pr} = 0$ .

Case 2: the pump pulse is also used as the probe pulse in two-pulse CARS, and phase shaping of the pump pulse is conducted to maximize the resonant signal at  $\omega_{as} = 0$ . In this case, the resonant signal is

$$P_{\rm r} = \frac{1}{\Delta^{3.2}} \int_{-\infty}^{\infty} \frac{C}{\omega_{\rm pr} - i\Gamma} e^{-\frac{3\omega_{\rm pr}^2}{2\Delta^2} + i\Phi_{\rm p}(\omega_{\rm pr})} \int_{-\infty}^{\infty} e^{-\frac{2(\omega_{\rm p} + \omega_{\rm pr}/2)^2}{2\Delta^2} + i\Phi_{\rm p}(\omega_{\rm pr})} d\omega_{\rm p} d\omega_{\rm pr} .$$

The numerical solution in Figure 5 shows that the optimal phase function is approximately a superposition of the linear and  $\arctan(\omega_{\rm pr}/\Gamma)/2$  phases: the optimal phase is quasi-linear away from  $\omega_{\rm p} = 0$  and similar to  $\arctan(\omega_{\rm pr}/\Gamma)/2$  around  $\omega_{\rm p} = 0$ . This can be understood as follows: since the zero phase profile (linear) is

optimal for  $|\int_{-\infty}^{\infty} e^{-\frac{2(\omega_{\rm p}+\omega_{\rm pr}/2)^2}{2\Delta^2}+i\Phi_{\rm p}(\omega_{\rm pr})} d\omega_{\rm p}|$ , and the  $\arctan(\omega_{\rm p}/\Gamma)$  phase is optimal for

 $\left|\int_{-\infty}^{\infty} \frac{C}{\omega_{\rm pr} - i\Gamma} e^{-\frac{3\omega_{\rm pr}^2}{2\Delta^2} + i\Phi_{\rm p}(\omega_{\rm pr})} d\omega_{\rm pr}\right|, \text{ then an approximate superposition of the linear and}$ 

 $\arctan(\omega_{\rm p}/\Gamma)$  functions will maximize  $|P_{\rm r}|$ .





Case 3: The probe pulse is shaped to control the signal-background difference at  $\omega_{as} = 0$ . In the lab, the signal and background are always detected together. Thus we have to enhance the resonant signal and suppress the non-resonant background simultaneously, which is a multi-objective optimization problem. It is better to choose the signal-background difference as the objective functional than the signal-to-background ratio, since the ratio will become infinite when  $|P_{nr}|=0$  no matter how small  $|P_r|$  is. A weight factor can be introduced to place different importance on background elimination:  $J = |P_r|^2 - k |P_{nr}|^2$ .

With the variational method, the optimal phase for the probe pulse is  

$$\Phi_{\rm pr}(\omega_{\rm pr}) = \arctan\left(\frac{\omega_{\rm pr}}{\Gamma - \lambda \gamma(\omega_{\rm pr}^2 + \Gamma^2)}\right) + \theta$$

Here  $\lambda = k(\chi_{nr} / C)^2$ , and  $\gamma$  can be determined by iteratively solving the equation  $3r^2$ 

$$\gamma = \frac{\int_{-\infty}^{\infty} e^{-\frac{3x^2}{2\Delta^2}} \cos(\arctan(\frac{x}{\Gamma - \lambda\gamma(x^2 + \Gamma^2)}))dx}{\int_{-\infty}^{\infty} e^{-\frac{3x^2}{2\Delta^2}} \frac{1}{\sqrt{x^2 + \Gamma^2}} \sin(\arctan(\frac{x}{\Gamma - \lambda\gamma(x^2 + \Gamma^2)}) - \arctan(\frac{\omega_{\rm pr}}{\Gamma}) + \frac{\pi}{2})dx}$$

Case 4: All the three pulses can be shaped for broadband signal enhancement and background suppression. The control here is broadband optimal control. In this case, the following objective functional can be adopted  $J = I_{\rm r} - I_{\rm nr} = \int_{-\infty}^{\infty} |P_{\rm r}|^2 d\omega_{\rm as} - \int_{-\infty}^{\infty} |P_{\rm nr}|^2 d\omega_{\rm as}.$ 



Figure 6. The left panal: the optimal phase function for the probe pulse in broadband optimal control. They are shown together with different shaping strategies in the frequency and time domains, respectively. TLP means transform limited pulse (no phase shaping). The right panel: the resonant signal and non-resonant background spectra with different phase shaping schemes for the probe pulse in three-pulse CARS. The parameters are  $\Delta = 50 \text{ cm}^{-1}$ ,  $\Gamma = 4.8 \text{ cm}^{-1}$ . Reproduced from [Gao et al, 2012], with the permission of AIP Publishing.

Analytical solution is not possible here, and numerical simulations show that the optimal phase shaping configuration consists of unshaped pump and Stokes pulses and a shaped probe pulse as shown in Figure 6.

It can be seen that the time delay scheme, which is usually adopted in the experiments, has almost the best performance in suppressing the broadband non-resonant background.

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#### **Biographical Sketches**

**Feng Shuang** graduated from University of Science and Technology of China as a Ph.D in chemical physics in 2000. Then he worked as a post-doctoral researcher at Hong Kong University of Science and Technology. After that, he went to Princeton University as a post-doctoral research associate from 2001 to 2003, and then became a research staff member at Princeton University after 2004. In 2009, he was admitted into One Hundred Talent Program in Chinese Academy of Sciences, and worked as a professor at Institute of Intelligent Machines, Chinese Academy of Sciences. He is now the director of Robot Sensor and Human-Machine Interaction Laboratory at IIM. His main researches cover tactile sensors, quantum sensors, information acquisition, quantum control, and quantum measurement. His studies have shown some new insights on quantum control. Number of his scientific publications is more than 50

**Jixin Cheng** carried out his PhD study in University of Science and Technology of China from 1994 to 1998. After postdoctoral training in Yijing Yan's group at Hong Kong University of Science and Technology and Sunney Xie's group at Harvard University, Cheng joined Purdue University in 2003 as Assistant Professor. He was promoted to Associate Professor in 2009 and Full Professor in 2013 in the Weldon School of Biomedical Engineering and Department of Chemistry. His research lab develops label-free spectroscopic imaging tools and nanotechnologies for challenging applications in biology and medicine. His research has yielded over 140 peer-reviewed articles that have been cited more than 7000 times. His contribution to the research field is demonstrated as the organizer of 16 national symposia, over 120 invited talks, and as primary editor of the first book on Coherent Raman Scattering Microscopy (2012). His is a co-inventor of CARS microscopy which is now available through Olympus and Leica.

**Fang Gao** graduated from University of Science and Technology of China in 2010, earning his Ph.D in chemical physics. After that, he worked as an assistant professor at Institute of Intelligent Machines. In 2013, he was promoted to an associate professor. His research interests mainly focus on quantum sensors, quantum control and computation chemistry. He has successfully carried out studies on optimal coherent control of CARS (coherent anti-Stokes Raman scattering) and pathway dynamics in the optimal quantum control of rubidium. Number of scientific publications is more than 20.

**Yaoxiong Wang** graduated from Northwestern University (China) in 2009, with a master degree in physics. After that, he joined Institute of Intelligent Machines, and became an assistant professor from 2012. His research interest includes quantum measurement, quantum control and compressive sensing. He has studied the optimal quantum measurement of finite-dimensional systems and perfect state transfer in spin chains. Number of scientific publications is more than 10.

**Dewen Cao** is now a Ph.D student under the supervision of Prof. Feng Shuang. His research mainly includes quantum control and quantum dissipation theory.

