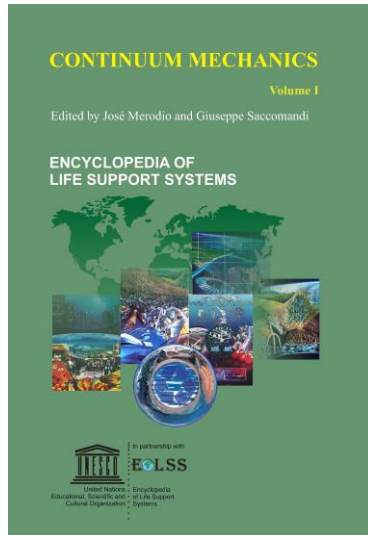


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## CONTINUUM MECHANICS



### **Continuum Mechanics Volume 1**

e-ISBN: 978-1-84826-372-7

ISBN : 978-1-84826-822-7

No. of Pages: 460

### **Continuum Mechanics Volume 2**

e-ISBN: 978-1-84826-373-4

ISBN : 978-1-84826-823-4

No. of Pages: 446

### **Continuum Mechanics Volume 3**

e-ISBN: 978-1-84826-374-1

ISBN : 978-1-84826-824-1

No. of Pages: 388

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